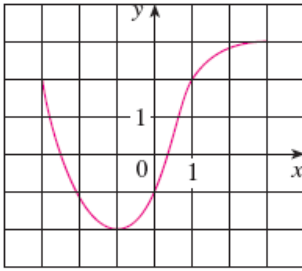


## Week 1 Friday Homework (1267029)

Question 12345678910111213141516171819202122  
 Due: Fri Sep 10 2010 09:00 PM EDT

1. Question DetailsSCalcET6 1.1.001. [667289]  
 The graph of a function  $f$  is given.



(a) State the value of  $f(1)$ .

(b) Estimate the value of  $f(2)$ .

(c) For what values of  $x$  is  $f(x) = 2$ ?

(smaller value)

(larger value)

(d) Estimate the values of  $x$  such that  $f(x) = 0$ .

(smaller value)

(larger value)

(e) State the domain and range of  $f$ .



] domain



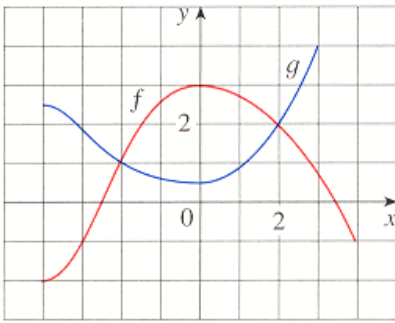
] range

(f) On what interval is  $f$  increasing?



]

2. Question DetailsSCalcET6 1.1.002. [657277]  
The graphs of  $f$  and  $g$  are given.



- (a) State the values of the functions below.

$$f(-4) = \boxed{\phantom{000}}$$

$$g(3) = \boxed{\phantom{000}}$$

- (b) For what values of  $x$  is  $f(x) = g(x)$ ?

$$\boxed{\phantom{000}} \text{ (smaller value)}$$

$$\boxed{\phantom{000}} \text{ (larger value)}$$

- (c) Estimate the solutions of the equation  $f(x) = -1$ .

$$x = \boxed{\phantom{000}} \text{ (smaller value)}$$

$$x = \boxed{\phantom{000}} \text{ (larger value)}$$

- (d) On what interval is  $f$  decreasing?

$$[ \boxed{\phantom{000}}, \boxed{\phantom{000}} ]$$

- (e) State the domain and range of  $f$ .

$$[ \boxed{\phantom{000}}, \boxed{\phantom{000}} ] \text{ domain}$$

$$[ \boxed{\phantom{000}}, \boxed{\phantom{000}} ] \text{ range}$$

- (f) State the domain and range of  $g$ .

$$[ \boxed{\phantom{000}}, \boxed{\phantom{000}} ] \text{ domain}$$

$$[ \boxed{\phantom{000}}, \boxed{\phantom{000}} ] \text{ range}$$

3. Question DetailsSCalcET6 1.1.021. [1289793]

If  $f(x) = 4x^2 - x + 5$ , find the following.

$$(a) f(2) = \boxed{\phantom{000}}$$

$$(b) f(-2) = \boxed{\phantom{000}}$$

$$(c) f(a) = \boxed{\phantom{000}}$$

$$(d) f(-a) = \boxed{\phantom{000}}$$

$$(e) f(a + 1) = \boxed{\phantom{000}}$$

$$(f) 2f(a) = \boxed{\phantom{000}}$$

$$(g) f(2a) = \boxed{\phantom{000}}$$

$$(h) f(a^2) = \boxed{\phantom{000}}$$

$$(i) [f(a)]^2 = \boxed{\phantom{000}}$$

$$(j) f(a + h) = \boxed{\phantom{000}}$$

**4.** Question DetailsSCalcET6 1.1.022. [1288853]

A spherical balloon with radius  $r$  inches has volume defined by the function below. Find a function that represents the amount of air required to inflate the balloon from a radius of  $r$  inches to a radius of  $r + 1$  inches. (Give the answer in terms of  $\pi$  and  $r$ .)

$$V(r) = \frac{4}{3}\pi r^3$$

**5.** Question DetailsSCalcET6 1.1.023. [1289645]

Consider the function below.

$$f(x) = 4 - 3x - x^2$$

Evaluate the difference quotient for the given function. Simplify your answer.

$$\frac{f(1+h) - f(1)}{h}$$

**6.** Question DetailsSCalcET6 1.1.025. [1289617]

Consider the function below.

$$f(x) = \frac{1}{x}$$

Evaluate the difference quotient for the given function. Simplify your answer.

$$\frac{f(x) - f(a)}{x - a}$$

**7.** Question DetailsSCalcET6 1.1.026. [1288740]

Consider the function below.

$$f(x) = \frac{x+7}{x+5}$$

Evaluate the difference quotient for the given function. Simplify your answer.

$$\frac{f(x) - f(5)}{x - 5}$$

**8.** Question DetailsSCalcET6 1.1.027. [667212]

Find the domain of the function. (Enter your intervals in ascending order. If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

$$f(x) = \frac{x}{4x-1}$$

    $\cup$    
**9.** Question DetailsSCalcET6 1.1.030. [656997]

Find the domain of the function. (If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

$$g(u) = \sqrt{u} + \sqrt{4-u}$$

  
**10.** Question DetailsSCalcET6 1.1.035. [667241]

Find the domain of the function. (If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

$$f(t) = t^2 - 9t$$

  
**11.** Question DetailsSCalcET6 1.1.039. [667274]

Find the domain of the function. (Enter your intervals in ascending order. If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

$$G(x) = \frac{6x + |x|}{x}$$

    $\cup$    
**12.** Question DetailsSCalcET6 1.1.045. [1289747]

Find an expression for the function whose graph is the line segment joining the points  $(2, -2)$  and  $(6, 4)$ . (Assume that these points are in the form  $(x, f(x))$ .)

$$f(x) = \text{[ ]} , \text{[ ]} \leq x \leq \text{[ ]}$$

13. Question DetailsSCalcET6 1.1.051. [1288682]

A rectangle has perimeter 10 m. Express the area of the rectangle as a function of the length ( $L$ ) of one of its sides.

$A(L) =$

State its domain. (If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

? ,  ?

14. Question DetailsSCalcET6 1.1.055. [1288360]

An open rectangular box with volume  $7 \text{ m}^3$  has a square base.

(a) Express the surface area of the box as a function of the length ( $x$ ) of a side of the base.

$SA(x) =$

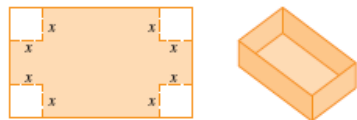
(b) State its domain. (If you need to use  $-\infty$  or  $\infty$ , enter -INFINITY or INFINITY.)

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15. Question DetailsSCalcET6 1.1.057. [1288167]

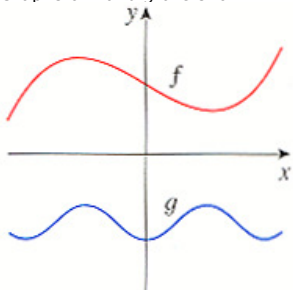
A box with an open top is to be constructed from a rectangular piece of cardboard with dimensions 18 in. by 30 in. by cutting out equal squares of side  $x$  at each corner and then folding up the sides as in the figure. Express the volume  $V$  of the box as a function of  $x$ .

$V =$



16. Question DetailsSCalcET6 1.1.062. [657096]

Graphs of  $f$  and  $g$  are shown.



(a) Is  $f$  even or odd?

- even  
 odd  
 neither

(b) Is  $g$  even or odd?

- even  
 odd  
 neither

17. Question DetailsSCalcET6 1.1.063. [667254]

(a) If the point  $(2, 6)$  is on the graph of an even function, what other point must also be on the graph?

( ,  )

(b) If the point  $(2, 6)$  is on the graph of an odd function, what other point must also be on the graph?

( ,  )

## 18. Question DetailsSCalcET6 1.1.066. [667242]

Determine whether  $f$  is even, odd, or neither. If you have a graphing calculator, use it to check your answer visually.

$$f(x) = \frac{x^2}{x^4 + 7}$$

- even  
 odd  
 neither

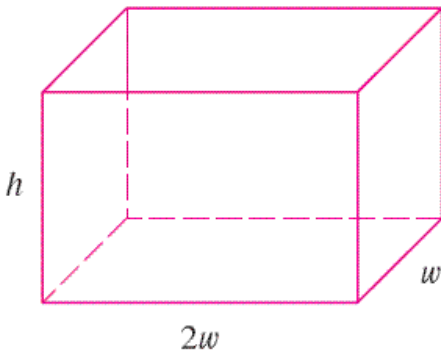
## 19. Question DetailsSCalcET6 1.1.069. [667278]

Determine whether  $f$  is even, odd, or neither. If you have a graphing calculator, use it to check your answer visually.

$$f(x) = 1 + 7x^2 - x^4$$

- even  
 odd  
 neither

## 20. Question DetailsSCalcET6 1.1.AE.05. [667290]



[Video Example](#)

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**EXAMPLE 5** A rectangular storage container with an open top has a volume of  $18 \text{ m}^3$ . The length of its base is twice its width. Material for the base costs  $\$8$  per square meter; material for the sides costs  $\$7$  per square meter. Express the cost of materials as a function of the width of the base.

**SOLUTION** We draw a diagram as in the figure and introduce notation by letting  $w$  and  $2w$  be the width and length of the base, respectively, and  $h$  be the height.

The area of the base is  $(2w)w = 2w^2$ , so the cost, in dollars, of the material for the base is  $\square (2w^2)$ . Two of the sides have area  $wh$  and the other two have area  $2wh$ , so the cost of the material for the sides is  $7[2(\square) + 2(2\square)]$ . The total cost is therefore

$$C = \square (2w^2) + 7[2(\square) + 2(2\square)] \\ = \square w^2 + \square wh$$

To express  $C$  as a function of  $w$  alone, we need to eliminate  $h$  and we do so by using the fact that the volume is  $18 \text{ m}^3$ . Thus

$$w(2w)h = \square$$

which gives

$$h = \frac{\square}{2w^2} = \frac{\square}{w^2}$$

Substituting this into the expression for  $C$ , we have

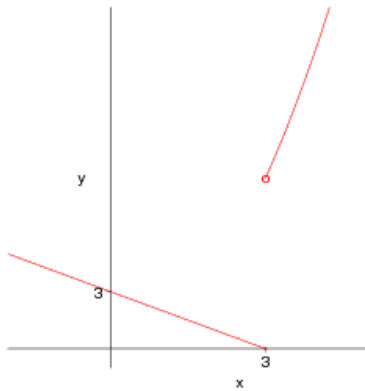
$$C = \square w^2 + \square w \left( \frac{\square}{w^2} \right) \\ = (\square)w^2 + \frac{\square}{w}$$


Therefore the equation

$$C = \square w^2 + \frac{\square}{w} \quad w > 0$$

expresses  $C$  as a function of  $w$ .

## 21. Question DetailsSCalcET6 1.1.AE.07. [1288351]



[Video Example](#) 

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**EXAMPLE 7** A function  $f$  is defined below.

$$f(x) = \begin{cases} 3 - x & \text{if } x \leq 3 \\ x^2 & \text{if } x > 3 \end{cases}$$

Evaluate  $f(0)$ ,  $f(3)$ , and  $f(7)$  and sketch the graph.

**SOLUTION** Remember that a function is a rule. For this particular function the rule is the following: First look at the value of the input  $x$ . If it happens that  $x \leq 3$ , then the value of  $f(x)$  is

. On the other hand, if  $x > 3$ , then the value of  $f(x)$  is  .

Since  $0 \leq 3$ , we have  $f(0) = 3 - 0 = 3$ .

Since  $3 \leq 3$ , we have  $f(3) = 3 - 3 = 0$ .

Since  $7 > 3$ , we have  $f(7) = 7^2 = 49$ .

How do we draw the graph of  $f$ ? We observe that if  $x \leq 3$ , then  $f(x) =$


, so the part of the graph of  $f$  that lies to the left of the vertical line  $x = 3$  must

coincide with the line  $y =$   , which has slope  and  $y$ -intercept  .

If  $x > 3$ , then  $f(x) =$   , so the part of the graph of  $f$  that lies to the right of the

line  $x = 3$  must coincide with the graph of  $y =$   which is a parabola. This enables us to sketch the graph in the figure.

## 22. Question DetailsSCalcET6 1.1.AE.11. [1289601]

[Video Example](#) 

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**EXAMPLE 11** Determine whether each of the following functions is even, odd, or neither even or odd.

(a)  $f(x) = x^5 + x$

(b)  $g(x) = 1 - x^4$

(c)  $h(x) = 2x - x^4$

**SOLUTION**

$$\begin{aligned} \text{(a) } f(-x) &= (\text{input})^5 + (\text{input}) \\ &= (\text{input})^5 x^5 + (\text{input}) \\ &= \text{input} = -(\text{input}) \\ &= -f(x) \text{ for all } x \text{ in the domain of } f(x) \end{aligned}$$

So  $f$  is an odd function.

$$\begin{aligned} g(-x) &= 1 - (\text{input})^4 \\ &= \text{input} \\ &= g(x) \text{ for all } x \text{ in the domain of } g(x) \end{aligned}$$

So  $g$  is even.

$$\begin{aligned} \text{(c) } h(-x) &= 2(\text{input}) - (\text{input})^4 \\ &= \text{input} \end{aligned}$$

Since there are values of  $x$  in the domain of  $h$  such that  $h(-x) \neq h(x)$  and  $h(-x) \neq -h(x)$ , we conclude that  $h$  is neither even nor odd.

8/6/2010

Category: **Homework**

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