

Quadratics.

Name \_\_\_\_\_

1. Let  $y = x^2$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_.
2. Let  $y = (x - 2)^2$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_.
3. Let  $y = (x - 2)^2 + 5$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_.
4. Let  $y = x^2 - 4x + 9$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_. Hint: convince yourself, by multiplication, that the equation in number 3 is exactly the same as the equation in number 4. Therefore the answer is obvious.
  
5. Let  $y = x^2 + 6x - 1$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_. Hint: rewrite the equation so that it looks like the ones in 1 through 3. Start by noting that  $(x + 3)^2 = x^2 + 6x + 9$  and make the proper adjustment by subtracting 10 so that the equations are the same.
  
6. Let  $y = x^2 - 8x + 5$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_.

7. Let  $y = 2x^2 + 8x + 1$ . The smallest value that  $y$  can take on is \_\_\_\_\_, which it takes if  $x$  is \_\_\_\_\_. Hint: The leading coefficient is 2, which is somewhat annoying. So factor as  $y = 2(x^2 + 4x) + 1$  and proceed as before, or else divide everything by 2 since  $y$  will be the smallest when  $\frac{y}{2}$  is.

8. Let  $y = -x^2 + 4x + 1$ . Does  $y$  have a minimum value, or a maximum? \_\_\_\_\_  
9. Find it, and the value of  $x$  that produces it.

10. Let  $y = ax^2 + bx + c$ .  $y$  will have a minimum value if  $a$  is \_\_\_\_\_  
and a maximum if  $a$  is \_\_\_\_\_.  
11. Find it, and the value of  $x$  that produces it.