

36. The charge distribution in this problem is equivalent to that of an infinite sheet of charge with surface charge density $\sigma = 4.50 \times 10^{-12} \text{ C/m}^2$ plus a small circular pad of radius $R = 1.80 \text{ cm}$ located at the middle of the sheet with charge density $-\sigma$. We denote the electric fields produced by the sheet and the pad with subscripts 1 and 2, respectively. Using Eq. 22-26 for \vec{E}_2 , the net electric field \vec{E} at a distance $z = 2.56 \text{ cm}$ along the central axis is then

$$\begin{aligned} \vec{E} = \vec{E}_1 + \vec{E}_2 &= \left(\frac{\sigma}{2\epsilon_0} \right) \hat{k} + \frac{(-\sigma)}{2\epsilon_0} \left(1 - \frac{z}{\sqrt{z^2 + R^2}} \right) \hat{k} = \frac{\sigma z}{2\epsilon_0 \sqrt{z^2 + R^2}} \hat{k} \\ &= \frac{(4.50 \times 10^{-12} \text{ C/m}^2)(2.56 \times 10^{-2} \text{ m})}{2(8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2) \sqrt{(2.56 \times 10^{-2} \text{ m})^2 + (1.80 \times 10^{-2} \text{ m})^2}} \hat{k} = (0.208 \text{ N/C}) \hat{k} \end{aligned}$$