

6. The centers of mass (with centimeters understood) for each of the five sides are as follows:

$$\begin{aligned}(x_1, y_1, z_1) &= (0, 20, 20) && \text{for the side in the } yz \text{ plane} \\(x_2, y_2, z_2) &= (20, 0, 20) && \text{for the side in the } xz \text{ plane} \\(x_3, y_3, z_3) &= (20, 20, 0) && \text{for the side in the } xy \text{ plane} \\(x_4, y_4, z_4) &= (40, 20, 20) && \text{for the remaining side parallel to side 1} \\(x_5, y_5, z_5) &= (20, 40, 20) && \text{for the remaining side parallel to side 2}\end{aligned}$$

Recognizing that all sides have the same mass  $m$ , we plug these into Eq. 9-5 to obtain the results (the first two being expected based on the symmetry of the problem).

(a) The  $x$  coordinate of the center of mass is

$$x_{\text{com}} = \frac{mx_1 + mx_2 + mx_3 + mx_4 + mx_5}{5m} = \frac{0 + 20 + 20 + 40 + 20}{5} = 20 \text{ cm}$$

(b) The  $y$  coordinate of the center of mass is

$$y_{\text{com}} = \frac{my_1 + my_2 + my_3 + my_4 + my_5}{5m} = \frac{20 + 0 + 20 + 20 + 40}{5} = 20 \text{ cm}$$

(c) The  $z$  coordinate of the center of mass is

$$z_{\text{com}} = \frac{mz_1 + mz_2 + mz_3 + mz_4 + mz_5}{5m} = \frac{20 + 20 + 0 + 20 + 20}{5} = 16 \text{ cm}$$