

36. We apply Eq. 3-30 and Eq. 3-23.

(a)  $\vec{a} \times \vec{b} = (a_x b_y - a_y b_x) \hat{k}$  since all other terms vanish, due to the fact that neither  $\vec{a}$  nor  $\vec{b}$  have any  $z$  components. Consequently, we obtain  $[(3.0)(4.0) - (5.0)(2.0)]\hat{k} = 2.0\hat{k}$ .

(b)  $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y$  yields  $(3.0)(2.0) + (5.0)(4.0) = 26$ .

(c)  $\vec{a} + \vec{b} = (3.0 + 2.0)\hat{i} + (5.0 + 4.0)\hat{j} \Rightarrow (\vec{a} + \vec{b}) \cdot \vec{b} = (5.0)(2.0) + (9.0)(4.0) = 46$ .

(d) Several approaches are available. In this solution, we will construct a  $\hat{b}$  unit-vector and “dot” it (take the scalar product of it) with  $\vec{a}$ . In this case, we make the desired unit-vector by

$$\hat{b} = \frac{\vec{b}}{|\vec{b}|} = \frac{2.0\hat{i} + 4.0\hat{j}}{\sqrt{(2.0)^2 + (4.0)^2}}.$$

We therefore obtain

$$a_b = \vec{a} \cdot \hat{b} = \frac{(3.0)(2.0) + (5.0)(4.0)}{\sqrt{(2.0)^2 + (4.0)^2}} = 5.8.$$