151 Linear Mathematics

1. The straight line goes through the points (-3, 2) and (4, -1). Find the slope of the line. According to the formula $m = \frac{y_2 - y_1}{x_2 - x_1}$ we have $m = \frac{-1 - 2}{4 - (-3)} = \frac{-3}{7}$.

Review 1

2. Write a point-slope equation for the line from Problem 1.

If we know the slope *m* and a point (a,b) on the straight line we can write an equation in the point-slope form as y-b = m(x-a). If we use e.g. the point (-3,2) then we can write

$$y-2 = -\frac{3}{7}[x-(-3)]$$
 or $y-2 = -\frac{3}{7}(x+3)$.

3. Write the slope-intercept equation for the line from Problem 1.

We will solve the equation we got in the previous problem for *y*.

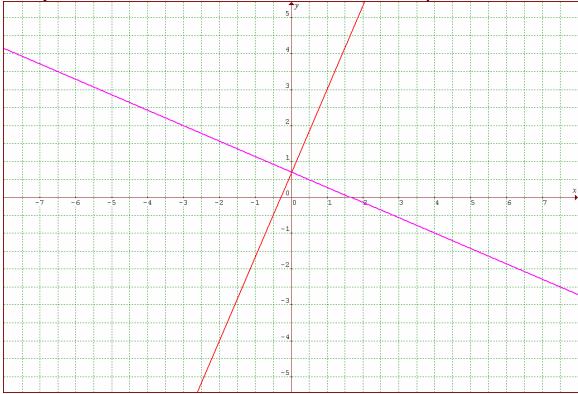
$$y = -\frac{3}{7}(x+3) + 2 = -\frac{3}{7}x - \frac{9}{7} + \frac{14}{7} = -\frac{3}{7}x + \frac{5}{7}.$$

4. Write an equation of the line parallel to the line from Problem 1 and going through the point (1,3).

Parallel lines have equal slopes and therefore we can write an equation of this parallel line in the point-slope form $y - 3 = -\frac{3}{7}(x-1)$. Solving for *y* we get an equation in the slope-intercept form $y = -\frac{3}{7}x + \frac{3}{7} + 3 = -\frac{3}{7}x + \frac{24}{7}$.

5. Write an equation of the line perpendicular to the line from Problem 1 and going through the point (1,3).

The slopes of perpendicular lines are negative reciprocals $(m_1m_2 = -1)$ and therefore the slope of the perpendicular line is $\frac{7}{3}$ and its equation in the point-slope form is $y-3 = \frac{7}{3}(x-1)$. Solving for y we get an equation in the slope-intercept form $y = \frac{7}{3}x - \frac{7}{3} + 3 = \frac{7}{3}x + \frac{2}{3}$.



6. Graph the lines from Problems 1 and 5 in the same coordinate system.

7. Find the point of intersection of the lines from Problems 1 and 5. We have to solve the system of equations

$$y = -\frac{3}{7}x + \frac{5}{7}$$
$$y = \frac{7}{3}x + \frac{2}{3}$$

Because the left parts are equal so are the right parts.

 $-\frac{3}{7}x + \frac{5}{7} = \frac{7}{3}x + \frac{2}{3}$. Multiplying both parts by the common denominator, 21, we get -9x + 15 = 49x + 14, or -58x = -1 and $x = \frac{1}{58}$. After we plug this value of x into the firs equation we get $y = -\frac{3}{7} \times \frac{1}{58} + \frac{5}{7} = \frac{287}{406} \approx .7$ 8. The straight line has the x-intercept -2 and the y-intercept 3. Write an equation of the

line. We use the formula $\frac{x}{a} + \frac{y}{b} = 1$ where *a* and *b* are the *x*-intercept and the *y*-intercept, respectively. In our case $\frac{x}{-2} + \frac{y}{3} = 1$ or 2y - 3x = 6.

9. If the price of a CD-player is \$40 the demand is 4000. If the price of the same CD- player is \$60 the demand is 3000. Assuming that the demand is a linear function of the price find the demand if the price is \$55.

First we need the slope-intercept equation of the line through the points (40, 4000) and

(60, 3000). The slope of the line is $m = \frac{3000 - 4000}{60 - 40} = \frac{-1000}{20} = -50$. Using for example

the first point we can write an equation of the line in the point-slope

form d - 4000 = -50(p - 40). From here, d = -50p + 6000. If

p = 55 then $d = -50 \times 55 + 6000 = 3250$.

10. A small company produces dolls. The permanent monthly expenses are \$6000 and the Cost of producing a doll is \$3. If the dolls sell for \$10 each what is the breakeven point?

The cost of producing x dolls is C(x) = 3x + 6000. The corresponding revenue

is R(x) = 10x. To find the break-even point we have to solve the equation R(x) = C(x),

or 10x = 3x + 6000. We have 7x = 6000 or $x = 6000/7 \approx 857$...